

JUN-2010

INDIAN INSTITUTE OF MATERIALS MANAGEMENT
Post Graduate Diploma in Materials Management
Graduate Diploma in Materials Management
PAPER - 2
QUANTITATIVE METHODS

Date: 13.06.2010
Time: 2.00pm to 5.00pm

Max. Marks: 100
Duration: 3 hours

Instructions:

- 1]. The question paper is in two parts- Part A: Objective Type (Compulsory) and Part B: Theory problems.
 - 2]. From part A, answer all questions. Each question carries 1 mark, total 25 marks.
 - 3]. From part B, answer any 5 questions out of 8 questions. Each question carries 15 marks, total 75 marks.
 - 4]. Use of calculator and/or mathematical table is permitted.
 - 5]. Graph sheet can be used wherever necessary.
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PART A

Q1. (A) State whether the following statements are true or false: (15 Marks)

- a). Allocation of optimum man-power to a particular job in order to minimize cost is a linear programming problem.
- b). A two variable LPP problem can be solved by Simplex method.
- c). If the constraints are inconsistent there is no feasible solution to a linear programming problem.
- d). Occupied cells in the transportation problem have no allocation.
- e). In an unbalanced transportation problem of minimization type zero cost is allocated to dummy cells.
- f). Loping and cycling are not faults in the network.
- g). An assignment problem cannot be solved by enumeration method.
- h). In a zero-sum game has actions that maximize expected gains and minimize expected loss.
- i). Total project duration on a network follows beta distribution.
- j). Kendall's notation can be used to represent a waiting line
- k). A pre-emptive priority is a static queue discipline.
- l). A buffer stock represents safety units of inventory against stock outs.

- m). Dynamic programming generates non-integer solutions to an LPP.
- n). Inter arrival time in a queue systems follows Poisson distribution.
- o). A normal distribution applies to a variable taking discrete values.

Q1. (B) Define the following: (10 Marks)

- a). Iso-profit line
- b). Unbounded solution
- c). Gomory cut
- d). Critical event
- e). Crashing

PART B

Q.2. (A). Cycle Trends is introducing two new lightweight bicycle frames, the Deluxe and the Professional, to be made from aluminum and steel alloys. The anticipated unit profits are Rs. 10 for the Deluxe and Rs. 15 for the Professional. The number of units of each alloy needed per frame is summarized in the table. A supplier delivers 100 units of the aluminum alloy and 80 units of the steel alloy weekly. Formulate this as a linear programming problem. **(5 Marks)**

Unit of each alloy needed per frame

| | Aluminum Alloy | Steel Alloy |
|--------------|----------------|-------------|
| Deluxe | 2 | 3 |
| Professional | 4 | 2 |

Q.2. (B). Solve the following LPP by graphical method

Maximize $Z = 10X_1 + 8X_2$

Subject to constraints

$2X_1 + X_2 \leq 20$

$X_1 + 3X_2 \leq 30$

$X_1 - 2X_2 \geq -15$

$X_1, X_2 \geq 0$

(10 Marks)

Q.3. A company has four manufacturing plants and five warehouses. Each plant manufactures the same product which is sold at different process in each warehouse area. The cost of manufacturing and the cost of raw material are different in each plant due to various factors.

The data is given in the table below:

| Item | Plant | | | |
|-------------------------------|-------|-----|-----|----|
| | 1 | 2 | 3 | 4 |
| Manufacturing Cost / unit Rs. | 12 | 10 | 8 | 8 |
| Raw Material Cost / unit Rs. | 8 | 7 | 7 | 5 |
| Capacity per unit time | 100 | 200 | 120 | 80 |

The company has five warehouses. The sale prices, transportation costs and demands are given in the following table:

| Warehouse | Transportation Cost (Rs.) per Unit | | | | Sale Price | Demand per Unit (Rs.) |
|-----------|------------------------------------|---|---|----|------------|-----------------------|
| | 1 | 2 | 3 | 4 | | |
| A | 4 | 7 | 4 | 3 | 30 | 80 |
| B | 8 | 9 | 7 | 8 | 32 | 120 |
| C | 2 | 7 | 6 | 10 | 28 | 150 |
| D | 10 | 7 | 5 | 8 | 34 | 70 |
| E | 2 | 5 | 8 | 9 | 30 | 90 |

- Compute the initial basic feasible solution using Vogel's Approximation Method. **(5 Marks)**
- Test the solution for optimality and find the optimal basic feasible solution and total transportation cost. **(10 Marks)**

Q.4. An electronic company manufactures small electrical devices. Products are manufactured on five different assembly lines (1,2,3,4,5). When manufacturing is finished, products are transported from the assembly lines to one of the five different inspection areas (A,B,C,D,E). Transporting products from five assembly lines to five inspection areas requires different times (in minutes) as shown in the table below:

(15 Marks)

| Assembly Line | Inspection Area | | | | |
|---------------|-----------------|----|----|----|----|
| | A | B | C | D | E |
| 1 | 10 | 4 | 6 | 10 | 12 |
| 2 | 11 | 7 | 7 | 9 | 14 |
| 3 | 13 | 8 | 12 | 14 | 15 |
| 4 | 14 | 16 | 13 | 17 | 17 |
| 5 | 19 | 11 | 17 | 20 | 19 |

Find the optimal assignment using Hungarian Method to optimize time.

Q.5. From the table of activities associated with the project given below:

- Draw the network
- Find the critical path
- Find the critical project duration.

| Activities | A | B | C | D | E | F | G | H | I |
|------------------|----|----|----|----|----|----|----|---|---|
| Optimistic time | 5 | 18 | 26 | 16 | 15 | 6 | 7 | 7 | 3 |
| Pessimistic time | 10 | 22 | 40 | 20 | 25 | 12 | 12 | 9 | 5 |
| Most likely time | 8 | 20 | 33 | 18 | 20 | 9 | 10 | 8 | 4 |

A, B, C are starting activities. B triggers F, A triggers E and D, F, E trigger I, D triggers H and C triggers G. H, I, J are end activities. **(15 Marks)**

Q.6.(A). Explain with an example sequencing. **(5 Marks)**

Q.6.(B). A book binder has one printing press, one binding machine and manuscripts of 7 different books. The times required for printing and binding operations are given in the following table:

| Book | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
|---------------|----|----|----|----|-----|----|----|
| Printing Time | 20 | 90 | 80 | 20 | 120 | 15 | 65 |
| Binding Time | 25 | 60 | 75 | 30 | 90 | 35 | 50 |

Determine the sequence will minimize the total time.

(10 Marks)

Q.7. **(5+10 Marks)**

On average 6 customers are served by a telephone booth every hour. What is the probability that a customer will have to wait at the booth and what is the average length of the queue? The length of telephone is exponential with a mean of 3 minutes.

Q.8. **(15 Marks)**

Solve the LPP using Simplex Method:

$$\text{Maximize } Z = 4X_1 + 3X_2$$

Subject to the constraints:

$$2X_1 + X_2 \leq 1000$$

$$X_1 \leq 400$$

$$X_2 \leq 700$$

$$X_1, X_2 \geq 0$$

Q.9. **(15 Marks)**

Solve the game graphically:

| | | Player B | |
|----------|----|----------|----|
| | | B1 | B2 |
| Player A | A1 | 1 | 2 |
| | A2 | 4 | 5 |
| | A3 | 9 | -7 |
| | A4 | -3 | -4 |
| | A5 | 2 | 1 |